

Forces & Moments

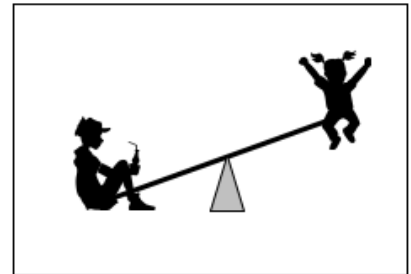
Balancing an Airplane

$$F = ma \quad \text{Force} = \text{mass} \times \text{acceleration}$$

$$M = T = rF \quad \text{Moment} = \text{Torque} = \text{distance} \times \text{Force}$$

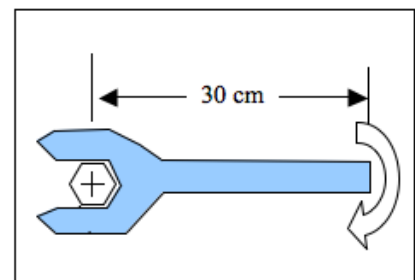
Seesaw Problem:

1. Jack and Jill are on a seesaw. Jack weighs 50 kg and sits 2 m from the **fulcrum** (pivot point). Jane weighs 30 kg. How far away must she sit to balance the seesaw?



Torque Problem:

2. Sandy has replaced the transmission on her 1983 Escort. The manual says the bolts must be tightened to 3 N•m. Her wrench is 30 cm long. What force should she apply?

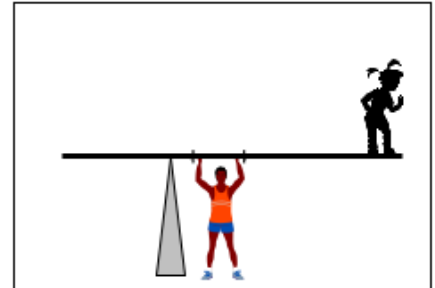


How much force should she apply if her wrench is 60 cm?

What happens if she torques the wrench too hard?

One-sided Seesaw:

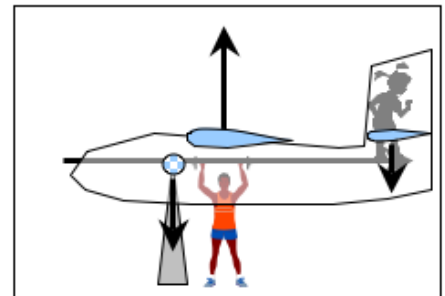
3. Let's look at a different kind of seesaw. Mr. Buff is pushing up 2400 N (≈ 540 lbf) 0.5 m to the right of the fulcrum. Jill (30 kg) is way off to the right. How far away must she be for the seesaw to balance?



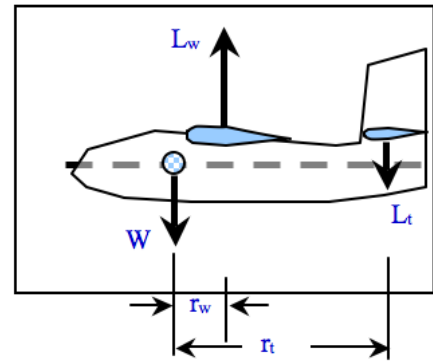
If Jill moves farther away, what will happen to the seesaw?

An airplane is essentially a one-sided seesaw.

4. The pivot point of an airplane is also known as the
 (a) center of gravity (c) rotation point
 (b) balance point (d) fulcrum
 The most correct is (a), all would be acceptable.
5. The weight acts through the
 (a) nose of the aircraft (c) center of gravity
 (b) wing center of lift (d) b and c
6. The wing generates
 (a) lift (c) more lift than drag
 (b) lift and drag (d) a, b, and c



7. Refer to the picture on the right. Identify the three **vertical** (up and down) forces acting on the airplane. [Use **W** for the weight arrow, **L_w** for wing lift, and **L_t** for tail lift.] Now, identify the two distances from the **center of gravity** (CG) to the wing center of lift [**r_w**] and to the tail center of lift [**r_t**].



8. What would happen to the nose of the airplane if the only forces were the weight and the wing lift?

What keeps this from happening?

9. The function of the horizontal tailplane is to
 (a) provide lift in the downward direction (c) keep the plane from pitching nose down
 (b) provide a means for longitudinal stability (d) all of the above
10. For an airplane to be balanced in cruise flight, both the net sum of the forces (ΣF) must be zero and the net sum of the moments (ΣM) must be zero.
 (a) Write the force-balance relationship.

$$\Sigma F = 0 \quad \text{convention: upward force is positive}$$

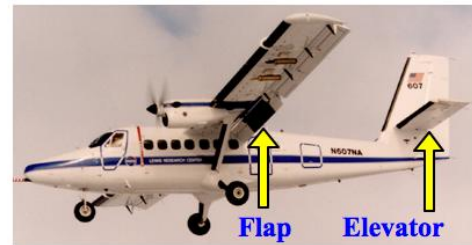
- (b) Write the moment-balance relationship. (**Hint:** It's easiest about the CG.)

$$\Sigma M = 0 \quad \text{convention: clockwise rotation is positive}$$

11. **BONUS:** Why is the CG forward of the wing center of lift?

12. **The Flaps** are extensions of the main wing near the fuselage (where people & cargo are). They are typically deployed during takeoff and landing. Their function is to increase the wing lift (L_w). Also, because they extend the chord of the wing, the center of lift moves aft (r_w increases).

The Elevator comprises the aft portion of the horizontal tailplane. The pilot deflects the trailing edge of the elevator both up and down by pulling and pushing on the control yoke, respectively. If the pilot pulls the elevator trailing edge up, the tailplane generates more downward lift.



NASA Glenn Icing Research Aircraft
DHC-6 Twin Otter

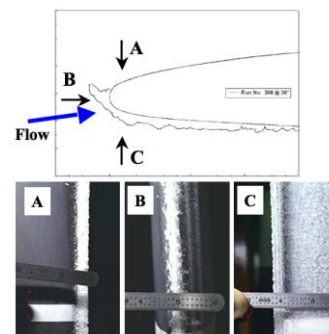


- (a) If flaps are deployed and nothing else changes, what happens to the nose of the aircraft?
- (b) If the pilot doesn't want that to happen, what compensation measures must be taken?

Now, let's consider a real life problem:

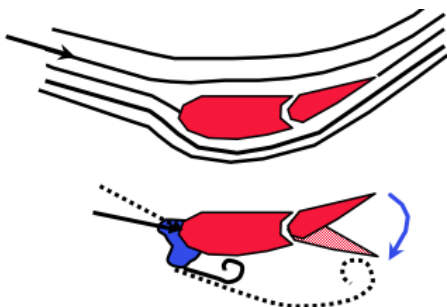
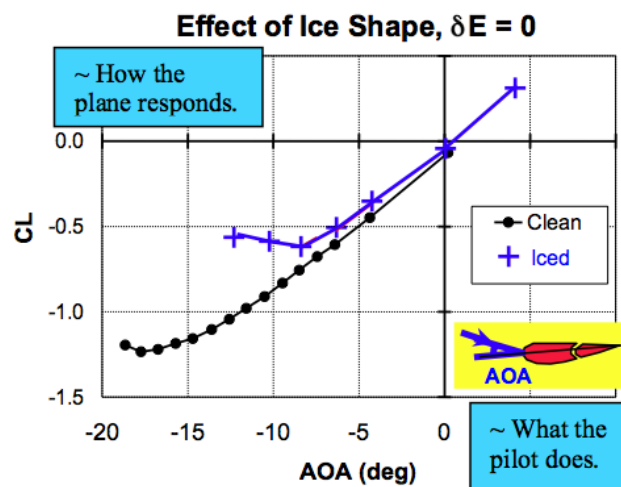
13. In certain weather conditions, ice begins to form on an airplane.
What parts of the airplane are critical to keep ice free?

14. To the right are a cross-sectional view and pictures of an ice-contaminated airfoil.



(a) What can happen to the pitch control (nose up and down movement) if flaps are deployed and the horizontal tailplane is contaminated with ice?

(b) How would the pilot use the elevator to compensate?



Clean Tailplane:
Attached, "smooth" flow

Iced Tailplane:
Separated flow
(A separation-induced elevator "snatch" is depicted.)